



COMPUTER AIDED DIAGNOSTIC FOR BACTERIAL CONTAMINATION IN DAIRY PRODUCTS USING SPECTRAL DATA PROCESSING AND MULTIVARIATE ANALYSIS

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ABSTRACT

The aim of the current research is to suggest clear, precise and quality methods regarding microbiological criteria for evaluating dairy products purity. The statistical models, which have been worked up for the classification of pathogenic microorganisms, are an instrument directed toward fulfilling the economic goals of analysis, which guarantees an evaluative mechanism permitting the maintenance of European and Bulgarian legislation related to European Union policies for the preservation of the public health.

Keywords food product hygiene, microbiological criteria for food purity, spectral and multivariate analysis

INTRODUCTION

European and Bulgarian legislation strives to provide regulations, connected to the general rules for the hygiene of food products in the respective member states. These rules are contained in the European Union's Common Agricultural Policy for the Preservation of Public Health, including Bulgaria as its member state¹. The reason for this is that some food products can threaten people's health, if specific rules connected with their hygienic production, storage and transportation and health labeling are not maintained.

Thus, a number of countries' strategies connected with increasing food safety have determined raw and ready-for-consumption products, in which traces of a variety of bacteria and toxic elements have been registered due to their multiplication, as dangerous to consumers [1, 2]. At the same time, monitoring indicates that approximately 5% of food ready for

consumption is contaminated with pathogenic microorganisms [3, 4]. A number of researchers describe cases of mass or sporadic poisoning with *Escherichia coli* and *Staphylococcus aureus* among others [5, 6, 7].

Striving towards a high level of public health protection is one of the main aims of the food law enacted via Regulation (EC) №1441/2007, related to microbiological criteria for food products. According to the law, food stuffs must not contain microorganisms or their metabolites in quantities, which present an unacceptable risk to human health.

The aforementioned regulation sets up mandatory testing of a series of types of pathogenic microorganisms and fixes criteria and norms for their presence in dairy products [8]. Main bacterial contamination in milk originates from the infected udder, the udder outside and from the equipment used in the milk storage and

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¹ Regulation (EC) №853/2004 of the European Parliament and the Council of the European Union from 29 April 2004 and its follow-up regulations 1290/2005 from 21 June 2005 and 119/2010 from 9 February 2010.

processing. Temperature, time and presence of nutrition are the most important factors affecting bacterial growth. Food stuffs produced from raw milk, or milk processed at lower pasteurization temperatures, conceal a serious risk of developing a variety of microorganisms. Raw milk contaminated with pathogenic microorganisms has decreased quality indicators, which leads to a sharp decline in the quality of the dairy products produced, a decrease in their length of freshness and a serious risk to human health.

Raw milk, which does not contain pathogenic bacteria, is called “safe”. According to Ordinance № 31 (BG) regarding the maximum acceptable quantity of contaminants in food, the presence of the pathogenic microorganisms *Staphylococcus aureus* and *Streptococcus agalactiae*, which are the subject of the current research, are “not permitted” in milk and dairy products.

Looked at as complex, polycomponent systems from the standpoint of their bacterial status, milk and dairy products may be the subject of modeling and research. The identification of the microorganisms, which cause bacterial infections, as well as the evaluation of milk and dairy product quality, based on microbiological, immunological and other such analyses are precise and objective, but also too laborious, lengthy, expensive and destructive. The necessity exists for faster, reliable methods and models to be developed, which would provide results equivalent to the classic methods, while allowing the testing of the raw materials and food stuffs not only in specialized laboratories, but also on location at the dairy farms, on the various food production lines, etc. That would then allow the respective corrective measures to be taken in a timely manner, directed toward protecting people’s health, while attaining the desired socioeconomic effect on the community. These methods may be of varied character, such as complex chemometric methods, multivariate analysis, pattern recognition analysis, etc. They allow precise measurements and a multifaceted, complex influence upon the various factors connected with the purity of food products. The interconnection between quantifying and qualifying factors is established. They assist, at the same time, in the evaluation of the influence

of the various microorganisms quickly and adequately.

One such method is spectral analysis in the near-infrared range (Near Infrared Spectroscopy – NIRS). Currently, a number of authors have reported positive results from using spectral analysis in the near-infrared range to ascertain the development of bacteria in various food stuffs [9, 10, 11, 12 and 13]. Its main advantages – speed (the analysis takes approximately one minute to complete), a lack of preliminary chemical preparation of the samples to be analyzed, the possibility to determine a number of components in the analyzed sample at once and the miniaturization of the measuring technology – have made it a good alternative to the classic methods of analysis. An immutable part of NIRS analysis is mathematical methods for quantitative and qualitative analysis. The development of mathematical methods for quality control, as well as computer technology allow the designing of new, effective instruments for quick processing and analysis of the data [14, 15 and 16]. The use of precise mathematical models creates the prerequisite indicators to perform analyses, without conditions and inaccuracies, which ensure speedy and objective diagnostics and guarantees certainty in relation to quality control of food stuffs without the subjective intervention of the researchers [17, 18].

The aim of this article is to suggest statistical regressive models for the ascertaining of the presence of a variety of types of pathogenic microorganisms in cow’s milk via the use of spectral analysis in the near-infrared range and the instrument of multivariate analysis.

MATERIALS AND METHODS

Experimental research

Two type of raw milk samples were used in the investigation – quarter foremilk samples and experimental set of milk samples, contaminated with *Staphylococcus aureus* and *Streptococcus agalactiae*.

Udder quarter foremilk samples were collected before morning milking from 37 Holstein dairy cows and were sampled twice a month for a nine months period. Bacteriological analysis of milk was performed by classical microbiological methods for detection of *Staphylococcus aureus*,

Streptococcus agalactiae. Laboratory procedures include subculturing onto selective Baird Parker agar and nonselective blood agar media as well Camp-test and biochemical tests for bacterial identification and differentiation.

Experimental set of milk samples were prepared by contaminating of 9.9 ml milk with 0.1 ml culture media containing from 10^2 CFU/ml to 10^{10} CFU/ml concentration of *Staphylococcus aureus* or *Streptococcus agalactiae* bacteria. A total of 35 milk samples were contaminated with *Staphylococcus aureus* and 34 samples with *Streptococcus agalactiae*, respectively. All samples were incubated for 24 hours at temperature 5°C before spectral measurement.

Classic microbiological analysis is used as a reference method to evaluate the accuracy of the developed models.

Spectral analysis

Near infrared spectra of all milk samples were obtained by NIRSystem 6500 spectrophotometer (FOSS NIRSystems, Silver Spring, MD, USA) in the spectral region from 600 to 1880 nm with 2 nm interval. The spectral data were collected as absorbance values [$\log(1/T)$], where T = transmittance. Before the spectral analysis, each sample was warmed up to 40°C in a water bath. The same temperature was maintenance during the spectra acquisition.

Spectra of the investigated samples are divided into classes as followed: samples contaminated with pathogenic bacteria (*Staphylococcus aureus* or *Streptococcus agalactiae*) are nominated as *Diseased* class, while the samples in which the presence of pathogenic bacteria is not established are declared as *Healthy* class. After that the milk samples contaminated with pathogenic bacteria (class *Diseased*) are divided additionally into two classes according to the type of bacteria: the samples which are contaminated with *Staphylococcus aureus* are nominated as *Staphylococcus* class, the samples contaminated with *Streptococcus agalactiae* are nominated as *Streptococcus* class.

The measured samples from each class are divided by a 3:1 ratio. Two thirds of them are used to form a calibration sample, while the others are used as test samples. Spectra from the calibration sample are used for the processing of

all of the classes described above. The models received are tested against the data from the test sample.

Models for measuring, analysis and evaluation

Normally, when measuring with a spectrophotometer, a vast quantity of measurement data is accumulated (319 samples, for each of which 606 spectral characteristics are received). In order to decrease the data without losing significant information the so-called Principal Component Analysis (PCA) is used. In this manner the data is compressed and, normally, with the use of 10-15 factors (Principal Components), all possible spectral variations are described. The use of that many factors allows the evaluation of their influence on the accuracy of the classification when varying their number. For this report the number of factors varies as follows: $x_j = 7,9,15$.

The program Pirouette 4.5 (Infometrics, Inc., Woodinville, WA, USA) was used for the processing of the spectral characteristics and the calculation of the Principal Components (PC).

During the exponential growth phase, microorganisms utilize sugars, proteins or lipids dissolved in the media to reproduce themselves. Biochemical changes in the foods properties and increasing bacterial biomass are the major consequences during the food storage time. Acquisition of the real bacterial count and biochemical changes in the foods are features related to the food safety and determining food shelf-life [19, 20].

The relationship between chemical changes in dairy products as a result of bacterial growth and the measured spectral data could be presented in a general form by the following relation:

$$\text{Bacterial status} = f(\text{spectral data}) + E(\text{error})$$

In some processes the combined influence of all the factors (Principal Components) observed is of substantial significance to the evaluation of their interdependence, as well as the result of their influence (increasing or decreasing) upon the sought after variables. The inclusion of all factors and the evaluation of their influence on the variables are made more difficult, if their number exceeds more than 5-6, due to their strong interdependence. So, in order to avoid

autocorrelation between them, specific models are sought out.

The interdependence between factors x_j , ($j=1,2,\dots,i$) where ($i=7,9,15$) and corresponding to class (Y) according to the type of bacteria is represented by a linear regressive model like:

$$Y_j = \alpha + \beta_0 \cdot x_j + \sum_{i=1}^j \beta_i \cdot f(x_{j-i}) + \varepsilon_j, \quad (1)$$

where:

Y_j – are the values of the dependent variables (the relevant class);

α, β_0, β_i – are the regression coefficients ($i=1,\dots,j$);

$f(x_j)$ – the reduced spectra to a number of major components (the independent variables).

The application of some other type of functional dependence – for example, logarithmic function – is impossible because some of the factors have negative values.

In the case of more independent variables, which is our case, it is possible that degeneration of the matrix with eigenvectors may occur. If the dependence is not complete, but statistically significant, then, theoretically, it is possible to discover parameters of the model (1) according to the Method of Least Squares [18]. It is possible, however, for a distortion in evaluating the parameters to occur and, as a result, the regressive equation (1) loses its informative meaning. In order to be able to discover the values of the regressive coefficients β_{j-1} ($j=1,2,\dots,i$), $i=7,9,15$ it is necessary to seek out other approaches, which rely upon assumptions [17].

In our case it is assumed that the factors are aligned according to the strength of influence from strongest to weakest, i.e. x_j, x_{j-1}, \dots, x_1 . With this assumption it is presumed that the coefficient β_0 is greater in value in comparison with the remaining coefficients. The anticipated decrease in the regressive coefficients may be subjected to various mathematical dependencies.

Two approaches are suggested, which form two mathematical models for identifying the presence of pathogenic bacteria in milk.

According to the first model it is assumed that the regressive coefficients β_{j-1} ($j=1,2,\dots,i$), $i=7,9,15$ decrease by arithmetic progression. Assuming that the reduction starts after a certain event, for example $i=1$ and at a certain value of β_1 , then the remaining values of the parameters β_i can be calculated at $i=2,3,\dots,14$ and $k \leq 15$ using the formula:

$$\beta_i = \beta_1 \left(1 - \frac{j-1}{k} \right), \quad (2)$$

If relation (2) is used, and the regression coefficients are substituted into equation (1), it takes the form:

$$Y = \alpha + \beta_0 \cdot x_j + \beta_1 \sum_{i=1}^j \left[1 - \frac{j-1}{k} \right] \cdot x_{j-i} + \varepsilon_j, \quad (3)$$

After labeling with $Z = \sum_{i=1}^j \left[1 - \frac{j-1}{k} \right] \cdot x_{j-i}$

equation (1) at $j=15$ for example becomes:

$$Y = \alpha + \beta_0 \cdot x_{15} + \beta_1 Z + \varepsilon_{15}, \quad (4)$$

With this summary the degree of influence of one of the factors is evaluated. That factor is assumed to be the most influential and assessing the impact of other factors is done by the aggregate variable Z_i .

According to the second model they decrease by geometric progression with the regression coefficient β_0 being the largest, followed by β_1 . They are subject to the following relation: $\beta_i = \beta_0 \cdot q^i$, where the dividend q fulfills the inequality $0 < q < 1$. Under these conditions, equation (1) can be represented like this:

$$Y_j = \alpha + \beta_0 \cdot x_j + \sum_{i=0}^j \beta_0 \cdot q^{i+1} \cdot x_{j-1}, \quad j=1 \div k, \quad (5)$$

To find the numerical values of the parameters α, β_0 and q the Method of least squares is applied again, but after a certain transformation known as "Koik's conversions" [21] to equation (5) it takes the form as a result:

$$Y_{15} = \gamma + q \cdot Y_{14} + \beta_0 \cdot x_{15} + \eta_{15}, \quad \text{where } \gamma = \alpha \cdot (1-q) \quad (6)$$

Equation (6) is a mixed model of regression and autoregression. It contains 3 regression coefficients γ , β_0 and q , whose numerical values are found using the Method of least squares. Finding q allows to determine all other regression coefficients and to establish the relationship between the factors and the relevant class.

Accepting that each of the factors could be of the greatest level of influence leads to receiving various combinations of regressive coefficients and various values for the variable Y in both types of models (arithmetic and geometric). That, in turn, leads to referring the variable Y toward one or the other of the conditionally labeled classes (*Diseased - Staphylococcus* or *Streptococcus* and *Healthy*) within the framework of the given confidence interval. Of all the possible combinations of regressive coefficients, depending on the various numbers of factors of influence upon the sought after variable Y , those in which the percentage of correctly classified samples is highest – according to both models for each separate class – are chosen.

For classification of samples confidence intervals are used, which are obtained by Student distribution [17, 18]:

$$\hat{Y} - t_{\alpha} \frac{\sigma}{\sqrt{n}} \leq Y \leq \hat{Y} + t_{\alpha} \frac{\sigma}{\sqrt{n}}, \quad (7)$$

where:

- t_{α} - is selected according to tabular degrees of freedom ($n-1$),

- $\sigma = \sqrt{\frac{\sum_{i=1}^n (Y_i - \bar{Y})^2}{n}}$ - is dispersion;

- n – number of observation data (samples).

According to the obtained values of \hat{Y} , the samples belong to one or another of the specified classes of these confidence intervals [22]:

- for class *Health* - $\hat{Y} \in (0.5; 1.5)$ and for class

Diseased - $\hat{Y} \in (1.51; 2.5)$;

- for class *Staphylococcus* - $\hat{Y} \in (4.00; 6.00)$ and

for class *Streptococcus* $\hat{Y} \in (6.01; 8.00)$.

In order to calculate the parameters of the models for classification and to seek the variables the STATISTICA 8.0 (StatSoft. Inc.) is used.

To provide faster operation of the analysis based on the received models a program code is developed in the environment of MatLab 6.5, which could be used in systems for automatic quality control of dairy products.

RESULTS

This research uses a total of 319 samples of cow milk. Via the classic methods of analysis it was determined that 173 of them were without the presence of pathogenic bacteria. 57 of the milk samples were infected with the *Staphylococcus aureus* and, respectively, another 89 samples were infected with *Streptococcus agalactiae*.

The selection of models we have suggested in various combinations (conditionally labeled as M_1, M_2, \dots, M_i , where $i=7,9,15$) of regressive coefficients is suitable according to the results displayed in the form of a table. In **Table 1** and **Table 2** are displayed the results for the models based on the assumption that the regressive coefficients decrease in arithmetic progression. The results for classes *Diseased* and *Healthy* are in **Table 1** and the results for classes *Staphylococcus* and *Streptococcus* are in **Table 2**, respectively. In **Table 3** and **Table 4** the results are displayed for the model based on the assumption that the regressive coefficients decrease in geometric progression – once again according to the two variants for division of the data.

It is obvious from the tables that the standard errors are small, i.e. the differences between the real and calculated values of the sought after variable are small.

Being that the experimental data were attained without iteration, in order to establish the adequacy of the model – that is, whether it can be used for a given type of research, the following null hypothesis is used (H_0): “the model is inadequate (does not explain anything)”. In other words, the regression causes such dispersion of the calculated values $\bar{Y}_j, j=1,2,\dots,N$ approximating the average arithmetic \bar{Y} , as is the dispersion of the test data $Y_j, j=1,2,\dots,N$ near \bar{Y} [18].

Table 1. Statistical model assuming that the coefficients decrease in arithmetic progression for classes Diseased and Healthy

model	α	β_0	β_1	R	R2	Sy	Dar-Wat	F
7 factors								
M ₁	0,639	0,029	-0,008	0,335	0,112	0,474	0,465	13,734
M ₂	0,377	0,057	0,259	0,315	0,099	0,477	0,489	11,995
M ₃	1,257	0,518	0,051	0,483	0,233	0,439	0,645	33,204
M ₄	0,131	-0,764	0,318	0,527	0,278	0,427	0,58	41,956
M ₅	-0,07	-0,982	0,363	0,454	0,206	0,448	0,595	28,266
M ₆	0,153	-0,784	0,311	0,384	0,147	0,464	0,526	18,838
M ₇	0,36	-0,588	0,262	0,318	0,101	0,477	0,495	12,239
9 factors								
M ₁	0,819	0,044	-0,809	0,461	0,213	0,446	0,605	29,425
M ₂	1,016	-0,112	0,288	0,422	0,178	0,456	0,533	23,586
M ₃	1,305	-0,393	0,127	0,432	0,187	0,453	0,57	25,041
M ₄	1,654	1,225	-0,059	0,584	0,34	0,408	0,618	56,271
M ₅	1,158	-0,824	0,201	0,396	0,157	0,462	0,502	20,225
M ₆	1,292	0,43	0,126	0,252	0,063	0,486	0,437	7,388
M ₇	1,302	1,418	0,121	0,273	0,074	0,486	0,439	8,756
M ₈	1,273	0,586	0,137	0,247	0,061	0,487	0,43	7,086
M ₉	1,279	-1,319	0,133	0,257	0,066	0,486	0,428	7,677
15 factors								
M ₁	1,479	-38,68	0,36	0,338	0,114	0,473	0,44	14,083
M ₂	1,472	-9,829	0,349	0,305	0,093	0,479	0,474	11,14
M ₃	1,475	-18,15	0,367	0,333	0,111	0,474	0,493	13,552
M ₄	1,469	-3,656	0,361	0,304	0,093	0,479	0,494	11,136
M ₅	1,469	3,103	0,36	0,304	0,092	0,479	0,468	11,072
M ₆	1,471	0,462	0,358	0,301	0,09	0,479	0,479	10,828
M ₇	1,471	-1,902	0,371	0,308	0,095	0,478	0,465	11,4
M ₈	1,468	-0,898	0,354	0,308	0,095	0,478	0,477	11,436
M ₉	1,468	-2,441	0,378	0,363	0,132	0,468	0,483	16,569
M ₁₀	1,471	-0,428	0,377	0,322	0,104	0,476	0,485	12,645
M ₁₁	1,471	-0,488	0,386	0,335	0,112	0,476	0,488	13,75
M ₁₂	1,481	-1,198	0,436	0,603	0,363	0,401	0,669	62,246
M ₁₃	1,471	0,118	0,382	0,324	0,105	0,476	0,489	12,744
M ₁₄	1,465	0,324	0,332	0,451	0,203	0,449	0,595	27,826
M ₁₅	1,475	0,028	-0,898	0,364	0,133	0,468	0,45	16,686

Table 2. Statistical model assuming that the coefficients decrease in arithmetic progression for classes Streptococcus and Staphylococcus

model	α	β_0	β_1	R	R ²	Sy	Dar-Wat	F
7 factors								
M ₁	10,335	-0,091	-0,25	0,314	0,098	1,49	0,455	11,889
M ₂	11,633	-0,277	-0,931	0,315	0,099	1,49	0,48	12,031
M ₃	8,696	-1,478	-0,243	0,457	0,209	1,392	0,599	28,772
M ₄	11,826	2,226	-0,984	0,51	0,26	1,347	0,549	38,323
M ₅	12,374	2,718	-1,107	0,433	0,187	1,411	0,551	25,153
M ₆	11,506	0,946	-0,902	0,333	0,111	1,476	0,492	13,608
M ₇	11,205	3,031	-0,831	0,335	0,112	1,475	0,479	13,798
9 factors								
M ₁	9,492	-0,124	2,08	0,413	0,171	1,425	0,544	22,459
M ₂	9,109	0,381	-0,9	0,431	0,185	1,413	0,514	24,816
M ₃	8,18	0,957	-0,378	0,367	0,134	1,456	0,515	16,918
M ₄	7,193	-3,453	0,144	0,532	0,283	1,326	0,56	42,993
M ₅	8,544	1,996	-0,562	0,339	0,115	1,473	0,479	14,169
M ₆	8,177	-2,646	-0,357	0,274	0,075	1,505	0,43	8,874
M ₇	8,156	-6,026	-0,348	0,289	0,084	1,499	0,449	9,943
M ₈	8,225	0,44	-0,386	0,235	0,055	1,522	0,431	6,377
M ₉	8,259	7,309	0,397	0,27	0,073	1,507	0,424	8,539
15 factors								
M ₁	7,667	54,43	-1,076	0,297	0,088	1,495	0,443	10,568
M ₂	7,671	77,579	-1,004	0,314	0,098	1,486	0,45	11,909
M ₃	7,656	95,604	-1,121	0,375	0,141	1,451	0,492	17,832
M ₄	7,687	27,35	-1,092	0,31	0,96	1,488	0,494	11,567
M ₅	7,685	-13,12	-1,08	0,295	0,087	1,496	0,45	10,403
M ₆	7,658	-26,48	-1,029	0,348	0,121	1,467	0,492	15,03
M ₇	7,676	8,214	-1,125	0,302	0,091	1,492	0,445	10,932
M ₈	7,69	5,62	-1,049	0,314	0,99	1,486	0,467	11,91
M ₉	7,687	9,38	-1,148	0,381	0,145	1,448	0,494	18,469
M ₁₀	7,687	1,183	-1,128	0,308	0,095	1,489	0,461	11,435
M ₁₁	7,679	0,1	-1,106	0,294	0,087	1,496	0,463	10,348
M ₁₂	7,651	3,216	-1,279	0,538	0,289	1,32	0,599	44,385
M ₁₃	7,678	-1,122	-1,164	0,308	0,095	1,489	0,462	11,406
M ₁₄	7,696	-1,015	-0,979	0,445	0,198	1,402	0,562	26,922
M ₁₅	7,669	-0,081	2,003	0,326	0,106	1,48	0,439	12,942

Table 3. Statistical model assuming that the coefficients decrease in geometric progression for classes Diseased and Healthy

model	γ	q	β_0	R	R2	Sy	Dar-Wat	F
7 factors								
M ₁	0,114	0,750	0,009	0,787	0,619	0,310	1,770	176,360
M ₂	0,354	0,765	-0,026	0,785	0,616	0,312	1,785	173,811
M ₃	0,409	0,722	0,130	0,787	0,620	0,310	1,771	177,026
M ₄	0,391	0,736	-0,298	0,791	0,625	0,306	1,774	181,068
M ₅	0,338	0,770	-0,197	0,783	0,613	0,313	1,808	171,727
M ₆	0,329	0,776	-0,163	0,782	0,611	0,313	1,809	170,579
M ₇	0,324	0,779	-0,267	0,781	0,611	0,314	1,801	170,175
9 factors								
M ₁	0,258	0,744	0,009	0,788	0,620	0,310	1,765	177,151
M ₂	0,322	0,781	6,1E-05	0,781	0,610	0,314	1,808	169,601
M ₃	0,370	0,751	-0,095	0,784	0,615	0,312	1,795	173,525
M ₄	0,532	0,662	0,438	0,803	0,646	0,299	1,703	197,630
M ₅	0,333	0,770	-0,175	0,783	0,614	0,312	1,808	172,373
M ₆	0,326	0,778	0,155	0,781	0,611	0,314	1,803	170,210
M ₇	0,335	0,773	0,606	0,783	0,613	0,313	1,786	171,833
M ₈	0,319	0,782	0,233	0,781	0,610	0,314	1,805	169,853
M ₉	0,323	0,779	-0,771	0,782	0,612	0,313	1,799	170,854
15 factors								
M ₁	0,336	0,775	-22,59	0,786	0,618	0,311	1,739	175,353
M ₂	0,327	0,779	-13,01	0,784	0,614	0,312	1,807	172,581
M ₃	0,329	0,777	-5,307	0,782	0,612	0,313	1,796	170,791
M ₄	0,310	0,790	5,736	0,784	0,615	0,312	1,799	173,157
M ₅	0,318	0,783	3,360	0,783	0,612	0,313	1,778	171,424
M ₆	0,322	0,781	0,149	0,781	0,610	0,314	1,809	169,609
M ₇	0,320	0,782	-1,464	0,782	0,612	0,313	1,801	171,126
M ₈	0,324	0,779	-0,622	0,782	0,611	0,313	1,801	170,668
M ₉	0,336	0,771	-0,893	0,784	0,615	0,312	1,777	173,035
M ₁₀	0,323	0,780	-0,083	0,781	0,610	0,314	1,809	169,785
M ₁₁	0,325	0,779	-0,109	0,781	0,610	0,314	1,808	170,042
M ₁₂	0,437	0,705	-0,425	0,795	0,633	0,305	1,770	186,881
M ₁₃	0,321	0,781	-0,004	0,781	0,610	0,314	1,808	169,604
M ₁₄	0,359	0,754	0,060	0,783	0,614	0,312	1,791	172,481
M ₁₅	0,367	0,750	0,008	0,787	0,619	0,310	1,770	176,242

Table 4. Statistical model assuming that the coefficients decrease in geometric progression for classes Streptococcus and Staphylococcus

model	γ	q	β_0	R	R2	Sy	Dar-Wat	F
7 factors								
M ₁	2,654	0,755	-0,027	0,788	0,622	0,965	1,771	178,196
M ₂	1,744	0,770	0,074	0,786	0,617	0,970	1,786	175,056
M ₃	2,077	0,729	-0,407	0,789	0,623	0,963	1,778	179,533
M ₄	1,969	0,743	0,915	0,792	0,628	0,957	1,791	183,106
M ₅	1,735	0,774	0,581	0,784	0,615	0,973	1,811	173,490
M ₆	1,671	0,783	0,051	0,783	0,613	0,976	1,810	171,552
M ₇	1,696	0,779	0,985	0,783	0,614	0,975	1,798	172,350
9 factors								
M ₁	2,288	0,749	-0,027	0,789	0,623	0,963	1,766	179,149
M ₂	1,692	0,780	0,019	0,783	0,613	0,976	1,808	171,705
M ₃	1,800	0,765	0,221	0,785	0,616	0,972	1,804	173,848
M ₄	2,303	0,687	-1,230	0,802	0,644	0,936	1,726	196,158
M ₅	1,727	0,777	0,411	0,784	0,615	0,973	1,819	173,158
M ₆	1,737	0,773	-0,994	0,785	0,616	0,972	1,795	174,118
M ₇	1,752	0,771	-2,033	0,785	0,616	0,972	1,793	174,112
M ₈	1,669	0,783	-0,052	0,783	0,613	0,976	1,809	171,543
M ₉	1,715	0,777	2,910	0,784	0,615	0,973	1,798	173,387
15 factors								
M ₁	1,660	0,782	48,363	0,785	0,616	0,972	1,777	174,270
M ₂	1,722	0,775	68,836	0,790	0,624	0,961	1,807	180,373
M ₃	1,772	0,768	30,424	0,786	0,618	0,969	1,776	175,546
M ₄	1,612	0,790	-10,319	0,784	0,614	0,974	1,813	172,712
M ₅	1,662	0,784	-14,053	0,786	0,617	0,971	1,787	174,882
M ₆	1,763	0,769	-9,657	0,786	0,618	0,970	1,810	175,298
M ₇	1,654	0,784	6,312	0,785	0,617	0,972	1,803	174,510
M ₈	1,715	0,777	2,277	0,784	0,615	0,974	1,802	173,014
M ₉	1,776	0,769	2,643	0,785	0,617	0,971	1,787	174,601
M ₁₀	1,677	0,782	0,282	0,783	0,613	0,976	1,808	171,765
M ₁₁	1,670	0,783	-0,122	0,783	0,613	0,976	1,808	171,600
M ₁₂	2,077	0,728	1,132	0,794	0,630	0,953	1,803	185,112
M ₁₃	1,662	0,784	0,080	0,783	0,613	0,976	1,808	171,691
M ₁₄	1,913	0,752	-0,228	0,787	0,619	0,969	1,788	175,979
M ₁₅	1,874	0,756	-0,025	0,788	0,621	0,965	1,772	178,030

Being that the values of the F-criteria are large ($F_{eq} > F_t$), the proposed H_0 is rejected and we can accept that the models we worked up in their great variety are adequate and can be used for analysis, evaluation and conclusions regarding the phenomena we studied.

The independent terms (α and γ) in the regressive coefficients of most models are larger than $\alpha = 0,05$. This means that their level of significance exceeds the standard error, i.e. they are statistically significant and, therefore the accepted H_0 is rejected. That allows us to conclude that we can use the Method of the Least Squares, the selection of models is suitable and they can be used for the needs of this research.

Of all the combinations of factors of influence upon the sought after variable in the models and for both types of assumptions regarding the regressive coefficients – regardless of whether they correspond to the requirements discussed above, those in which the percent of correctly classified samples were the highest for each separate class were chosen.

The classification results with the most suitable models (conditionally labeled M_1, M_2, \dots, M_i , where $i=7,9,15$) are presented in **Table 5** where the data are divided into classes *Diseased* and *Healthy* and **Table 6** where the data is divided into classes *Staphylococcus* and *Streptococcus* for the calibration and test samples, respectively.

Table 5. Classification of calibration and test set by dividing the sample into classes *Diseased* and *Healthy*, for both assumptions (arithmetical and geometrical reduction of regression coefficients)

Sample classes	Number of factors	Arithmetically decreasing coeff.			Geometrically decreasing coeff.		
		% Correct classifications			% Correct classifications		
		Model type	Calibration set	Test set	Model type	Calibration set	Test set
<i>Healthy</i>	7 factors	M ₃	74,36 %	36,84 %	M ₂	100 %	98,64 %
<i>Diseased</i>		M ₃	70,19 %	100 %	M ₃	84,26 %	93,18 %
<i>Healthy</i>	9 factors	M ₄	72,65 %	68,42 %	M ₂	87,15 %	91,04 %
<i>Diseased</i>		M ₄	89,42 %	68,09 %	M ₈	100 %	97,94%
<i>Healthy</i>	15 factors	M ₁₂	69,23 %	57,89 %	M ₁₀	72,56 %	70,16 %
<i>Diseased</i>		M ₁₂	91,35 %	89,36 %	M ₅	74,04 %	78,72 %

Table 6. Classification of calibration and test set by dividing the sample into classes *Staphylococcus* and *Streptococcus*, for both assumptions (arithmetical and geometrical reduction of regression coefficients)

Sample classes	Number of factors	Arithmetically decreasing coeff.			Geometrically decreasing coeff.		
		% Correct classifications			% Correct classifications		
		Model type	Calibration set	Test set	Model type	Calibration set	Test set
<i>Staphylococcus</i>	7 factors	M ₃	0 %	66,67 %	M ₃	92,87 %	98,14 %
<i>Streptococcus</i>		M ₁	95,16 %	100 %	M ₂	100 %	0 %
<i>Staphylococcus</i>	9 factors	M ₇	7,14 %	0 %	M ₆	57,14 %	33,33 %
<i>Streptococcus</i>		M ₃	100 %	96,25 %	M ₂	73,67 %	86,14 %
<i>Staphylococcus</i>	15 factors	M ₉	7,14 %	0 %	M ₅	28,57 %	16,67 %
<i>Streptococcus</i>		M ₁₂	100 %	93,12 %	M ₁₀	69,73 %	62,29 %

The results received indicate that the application of some mathematical models ensure 100% accuracy of classification of types of bacteria researched for milk, in both the calibration and test samples. At the same time, they provide a basis to believe that the influence of various types of factors on the classes may be measured, analyzed and evaluated via these models. In terms of faster operation of the analysis by dividing the sample into classes *Diseased* and *Healthy* the most appropriate is the geometric model M₂ working with 7 factors and ensuring 100% accuracy of classification for the calibration set and 98.64% accuracy for the test set. When dividing the sample into classes *Staphylococcus* and *Streptococcus* the most appropriate is the arithmetic model M₃ working with 9 factors and ensuring 100% accuracy for the calibration set and 96.25% accuracy for the test set, respectively.

CONCLUSIONS

The mathematical models designed to analyze the quality of milk and dairy products could be used as a good alternative to the classic methods for analyzing the development of bacteria in food stuffs. The suggested mathematical models allow quick and accurate evaluation of the

classification of various types of bacteria with extremely high precision with every alteration in the input data. The results received via this approach could be able to guarantee certainty regarding the quality control of food and the preservation of public health.

The approach is universal and can be applied to the evaluation of food stuffs from animals. The products, which answer to the criteria in the Regulations, will have no barrier to being sold. The food stuffs observed in accordance with Bulgarian standards will also correspond to international requirements. They will contribute to the creation of a domestic market, which will ensure a high level of preservation of public health in the country. At the same time, the European Union requirements for the preservation of the public health will be upheld and they will be able to freely enter the European market as desirable and quality food products.

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